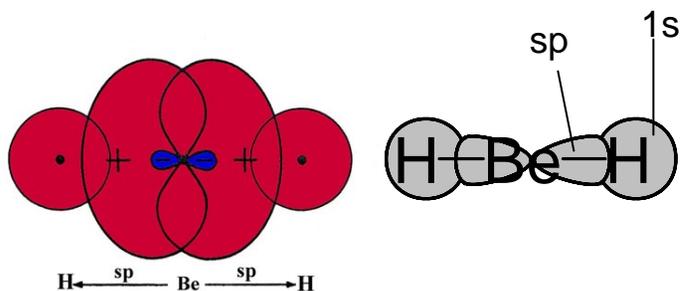




Chem 59-250 The Delocalized Approach to Bonding: Molecular Orbital Theory

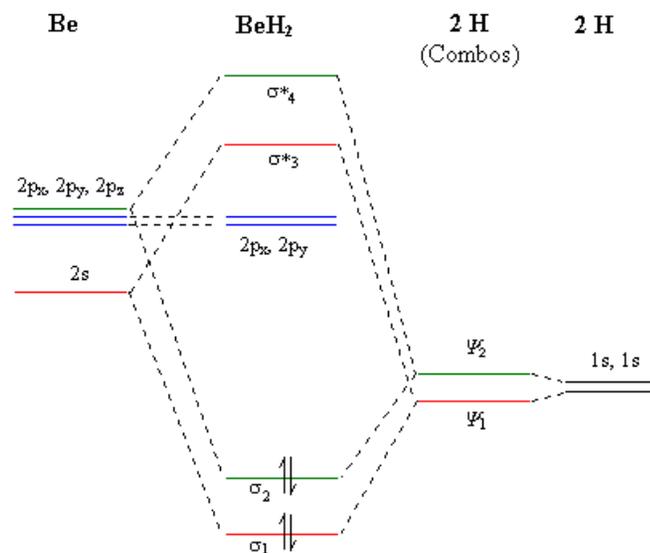
The localized models for bonding we have examined (Lewis and VBT) assume that all electrons are restricted to specific bonds between atoms or in “lone pairs”. In contrast, the delocalized approach to bonding places the electrons in Molecular Orbitals (MO's) - orbitals that encompass the entire molecule and are not associated with any particular bond between two atoms. In most cases, MO theory provides us with a more accurate picture of the electronic structure of molecules and it gives us more information about their chemistry (reactivity).

Localized Bonding

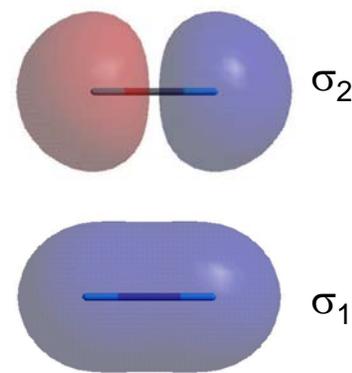


Two (sp-1s) Be-H σ bonds.

Delocalized Bonding



MO diagram for BeH₂



The two σ bonding MO's in BeH₂

Molecular orbitals are constructed from the available atomic orbitals in a molecule. This is done in a manner similar to the way we made hybrid orbitals from atomic orbitals in VBT. That is, we will make the MO's for a molecule from Linear Combinations of Atomic Orbitals (LCAO). In contrast to VBT, in MO theory the atomic orbitals will come from several or all of the atoms in the molecule. Once we have constructed the MO's, we can build an MO diagram (an energy level diagram) for the molecule and fill the MO's with electrons using the Aufbau principle.

Some basic rules for making MO's using the LCAO method:

- 1) n atomic orbitals must produce n molecular orbitals (e.g. 8 AO's must produce 8 MO's).
- 2) To combine, the atomic orbitals must be of the appropriate symmetry.
- 3) To combine, the atomic orbitals must be of similar energy.
- 4) Each MO must be normal and must be orthogonal to every other MO.

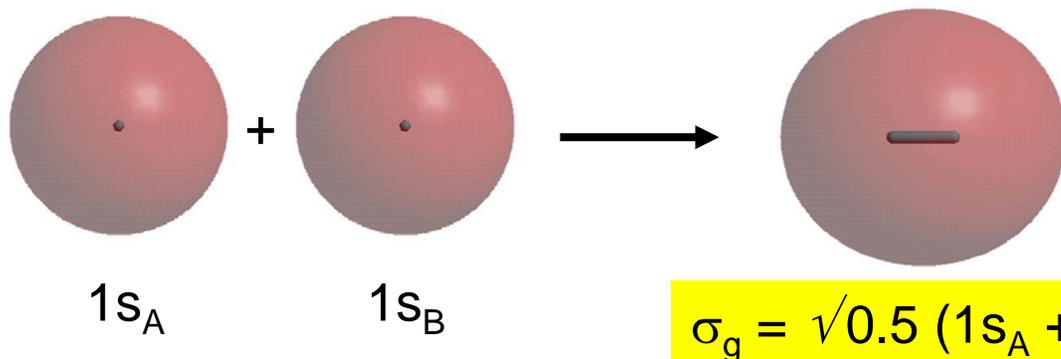




Diatomic molecules: The bonding in H₂

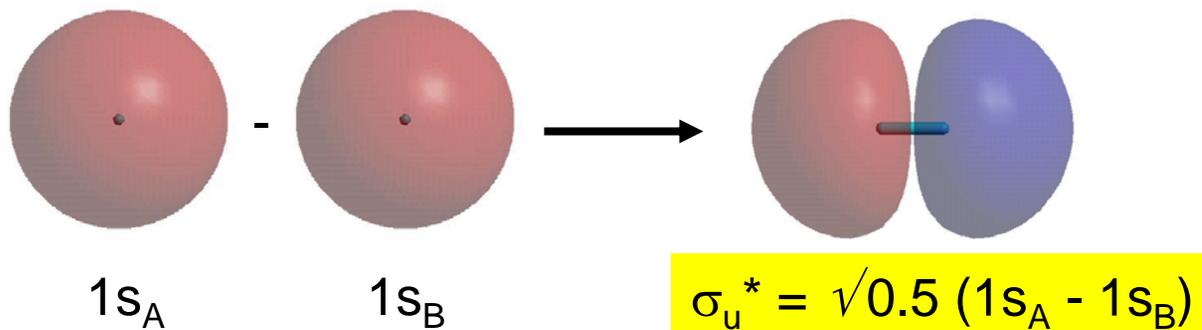
Each H atom has only a 1s orbital, so to obtain MO's for the H₂ molecule, we must make linear combinations of these two 1s orbitals.

Consider the addition of the two 1s functions (with the same phase):



This produces an MO around both H atoms and has the same phase everywhere and is symmetrical about the H-H axis. This is known as a *bonding* MO and is given the label σ_g because of its symmetry.

Consider the subtraction of the two 1s functions (with the same phase):



This produces an MO over the molecule with a node between the atoms (it is also symmetrical about the H-H axis). This is known as an *antibonding* MO and is given the label σ_u^* because of its symmetry. The star indicates antibonding.

Remember that:  is equivalent to: 

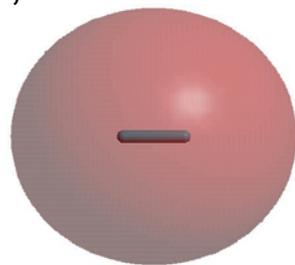
Chem 59-250 Molecular Orbital Theory



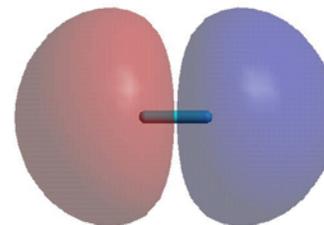
Diatomic molecules: The bonding in H_2

You may ask ... Why is σ_g called “bonding” and σ_u^* “antibonding”? What does this mean? How do you know the relative energy ordering of these MO’s?

Remember that each 1s orbital is an atomic wavefunction (ϕ_{1s}) and each MO is also a wave function, Ψ , so we can also write LCAO’s like this:



$$\sigma_g = \Psi_1 = \sqrt{0.5} (\phi_{1sA} + \phi_{1sB})$$



$$\sigma_u^* = \Psi_2 = \sqrt{0.5} (\phi_{1sA} - \phi_{1sB})$$

Remember that the square of a wavefunction gives us a probability density function, so the density functions for each MO are:

$$(\Psi_1)^2 = 0.5 [(\phi_{1sA} \phi_{1sA}) + \mathbf{2(\phi_{1sA} \phi_{1sB})} + (\phi_{1sB} \phi_{1sB})]$$

$$\text{and } (\Psi_2)^2 = 0.5 [(\phi_{1sA} \phi_{1sA}) - \mathbf{2(\phi_{1sA} \phi_{1sB})} + (\phi_{1sB} \phi_{1sB})]$$

The only difference between the two probability functions is in the cross term (in bold), which is attributable to the kind and amount of *overlap* between the two 1s atomic wavefunctions (the integral $\int (\phi_{1sA} \phi_{1sB}) \delta\tau$ is known as the “overlap integral”, S). In-phase overlap makes *bonding* orbitals and out-of-phase overlap makes *antibonding* orbitals...why?

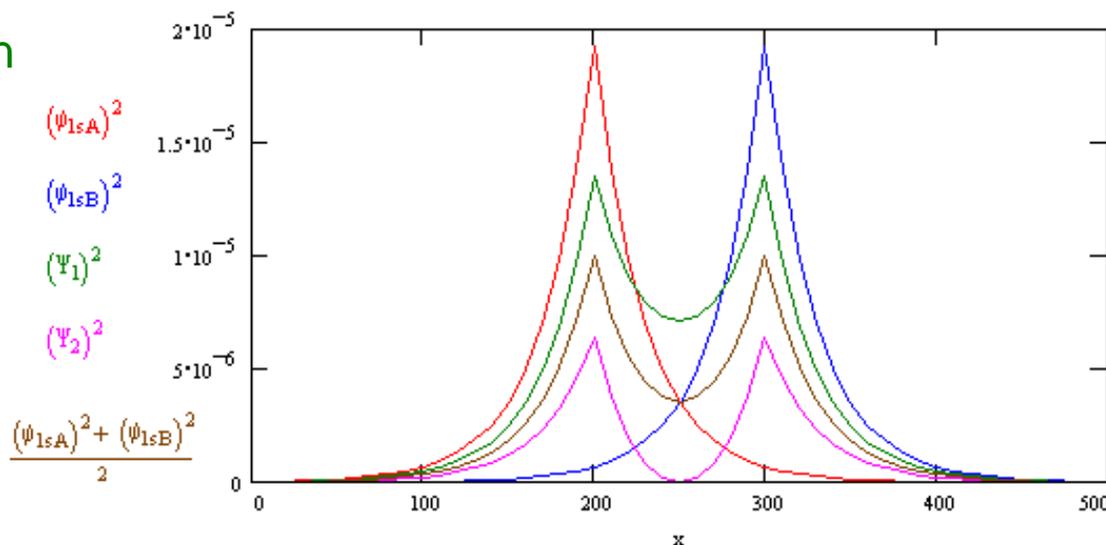


Diatomic molecules: The bonding in H_2

Consider the electron density between the two nuclei: the **red** curve is the probability density for H_A by itself, the **blue** curve is for H_B by itself and the **brown** curve is the density you would get for $\phi_{1sA} + \phi_{1sB}$ without any overlap: it is just $(\phi_{1sA})^2 + (\phi_{1sB})^2$ {the factor of $\frac{1}{2}$ is to put it on the same scale as the normalized functions}.

The function $(\Psi_1)^2$ is shown in **green** and has an extra $+ 2(\phi_{1sA} \phi_{1sB})$ of electron density than the situation where overlap is neglected.

The function $(\Psi_2)^2$ is shown in **pink** and has less electron density between the nuclei $\{- 2(\phi_{1sA} \phi_{1sB})\}$ than the situation where overlap is neglected.



$$(\Psi_1)^2 = 0.5 [(\phi_{1sA} \phi_{1sA}) + \mathbf{2}(\phi_{1sA} \phi_{1sB}) + (\phi_{1sB} \phi_{1sB})]$$

$$(\Psi_2)^2 = 0.5 [(\phi_{1sA} \phi_{1sA}) - \mathbf{2}(\phi_{1sA} \phi_{1sB}) + (\phi_{1sB} \phi_{1sB})]$$

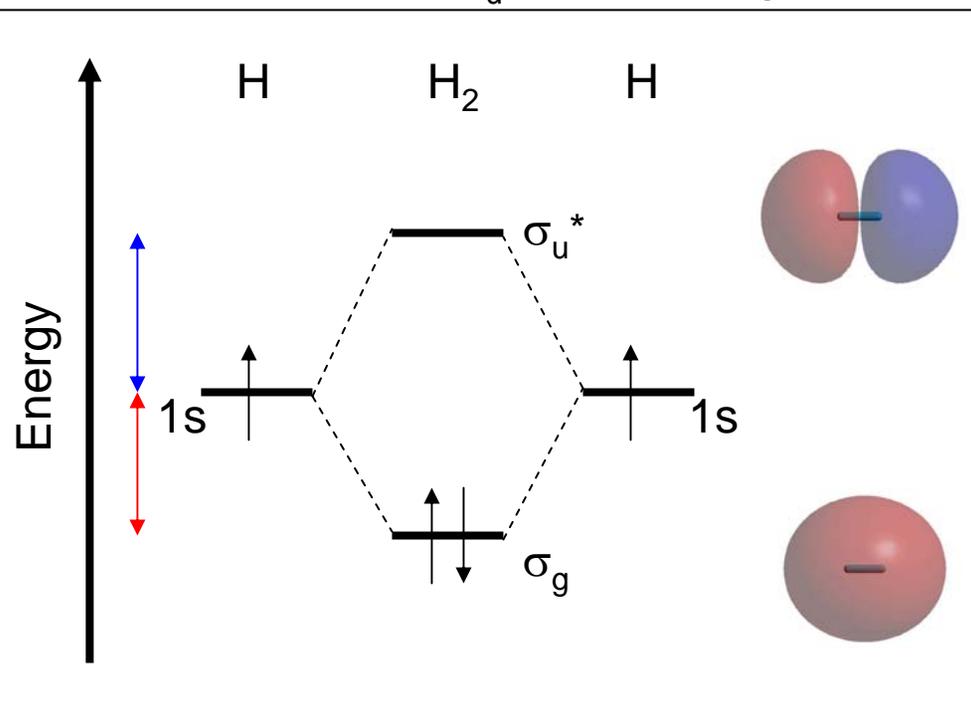
The increase of electron density between the nuclei from the in-phase overlap reduces the amount of repulsion between the positive charges. This means that a bonding MO will be lower in energy (more stable) than the corresponding antibonding MO or two non-bonded H atoms.

Chem 59-250 Molecular Orbital Theory

Diatomic molecules: The bonding in H₂



So now that we know that the σ bonding MO is more stable than the atoms by themselves and the σ_u^* antibonding MO, we can construct the MO diagram.



To clearly identify the symmetry of the different MO's, we add the appropriate subscripts g (symmetric with respect to the inversion center) and u (anti-symmetric with respect to the inversion center) to the labels of each MO.

The electrons are then added to the MO diagram using the Aufbau principle.

Note:

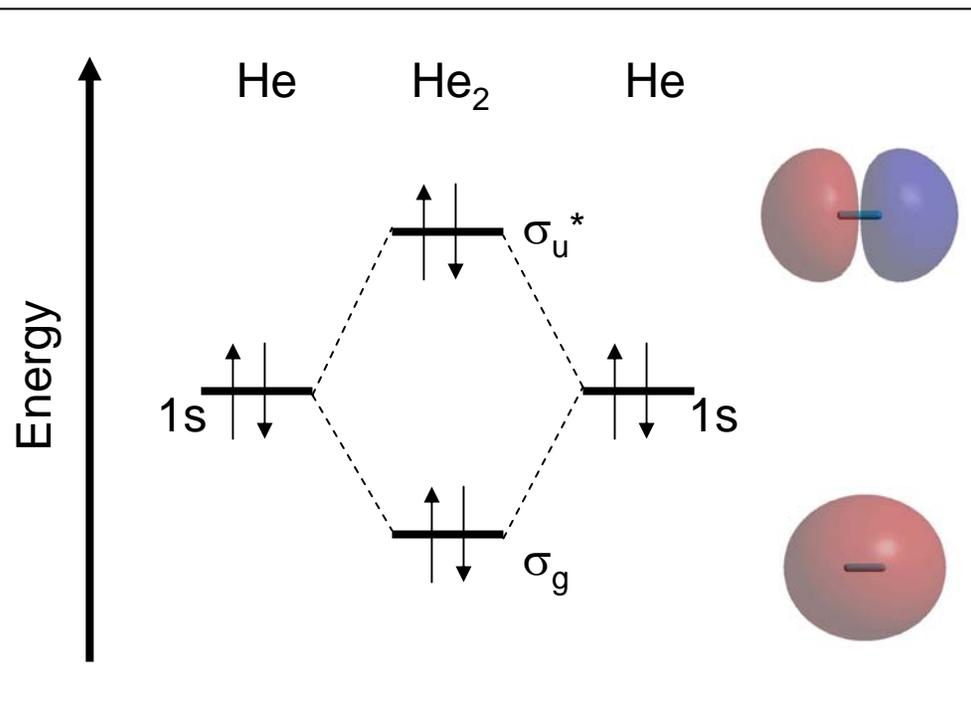
The amount of stabilization of the σ_g MO (indicated by the red arrow) is slightly less than the amount of destabilization of the σ_u^* MO (indicated by the blue arrow) because of the pairing of the electrons. For H₂, the stabilization energy is 432 kJ/mol and the bond order is 1.

$$\text{Bond Order} = \frac{(\# \text{ of } e^- \text{ in bonding MO's}) - (\# \text{ of } e^- \text{ in antibonding MO's})}{2}$$



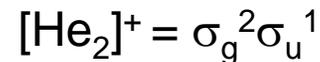
Diatomic molecules: The bonding in He₂

He also has only 1s AO, so the MO diagram for the molecule He₂ can be formed in an identical way, except that there are two electrons in the 1s AO on He.



The bond order in He₂ is $(2-2)/2 = 0$, so the molecule **will not exist**.

However the cation [He₂]⁺, in which one of the electrons in the σ_u^* MO is removed, would have a bond order of $(2-1)/2 = 1/2$, so such a cation might be predicted to exist. The electron configuration for this cation can be written in the same way as we write those for atoms except with the MO labels replacing the AO labels:

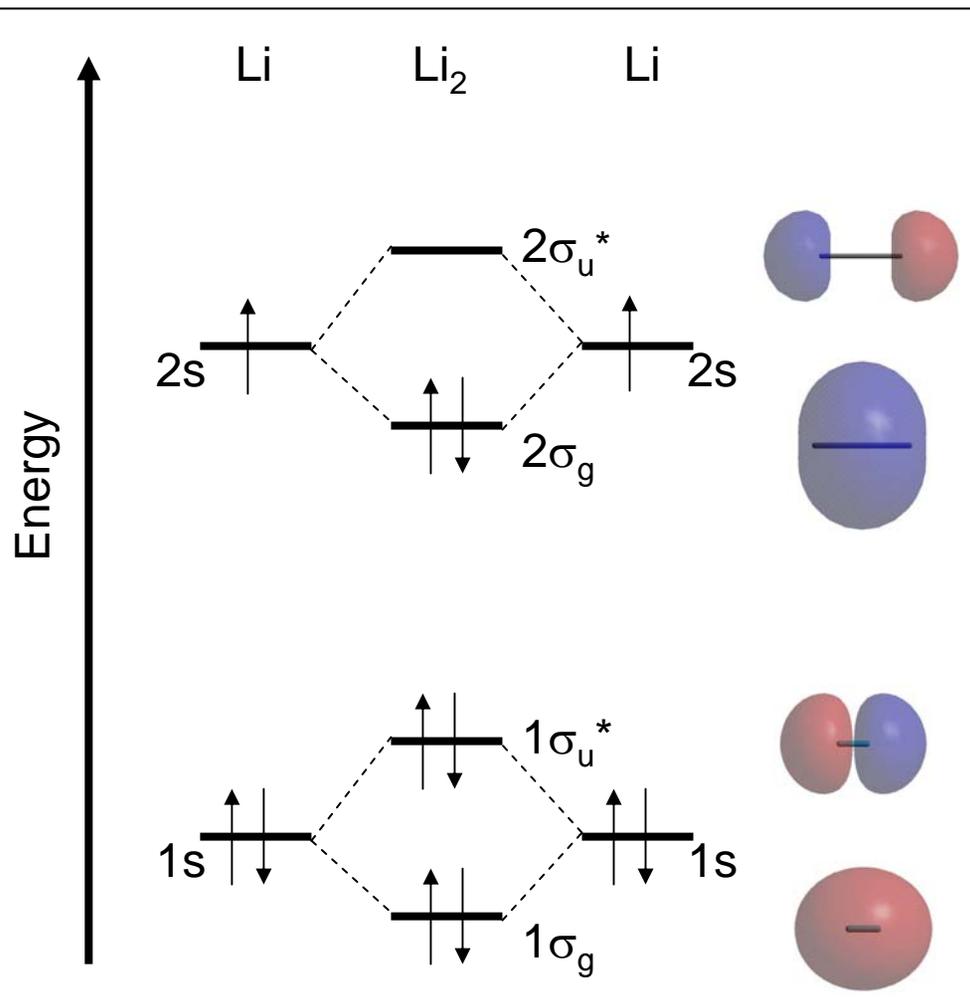


Molecular Orbital theory is powerful because it allows us to predict whether molecules should exist or not and it gives us a clear picture of the of the electronic structure of any hypothetical molecule that we can imagine.

Chem 59-250 Molecular Orbital Theory

Diatomic molecules: Homonuclear Molecules of the Second Period

Li has both 1s and 2s AO's, so the MO diagram for the molecule Li_2 can be formed in a similar way to the ones for H_2 and He_2 . The 2s AO's are not close enough in energy to interact with the 1s orbitals, so each set can be considered independently.



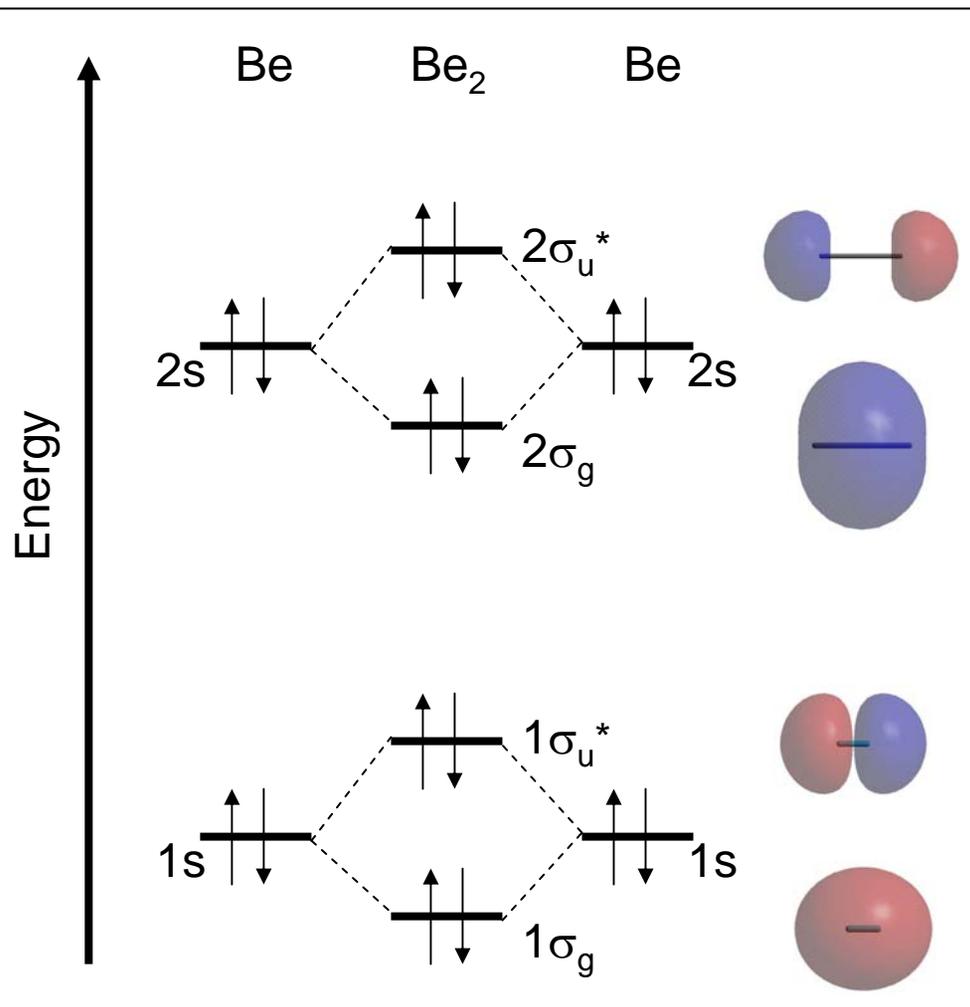
The bond order in Li_2 is $(4-2)/2 = 1$, so the molecule could exist. In fact, a bond energy of 105 kJ/mol has been measured for this molecule.

Notice that now the labels for the MO's have numbers in front of them - this is to differentiate between the molecular orbitals that have the same symmetry.

Chem 59-250 Molecular Orbital Theory

Diatomic molecules: Homonuclear Molecules of the Second Period

Be also has both 1s and 2s AO's, so the MO's for the MO diagram of Be_2 are identical to those of Li_2 . As in the case of He_2 , the electrons from Be fill all of the bonding and antibonding MO's so the molecule will not exist.



The bond order in Be_2 is $(4-4)/2 = 0$, so the molecule can not exist.

Note:

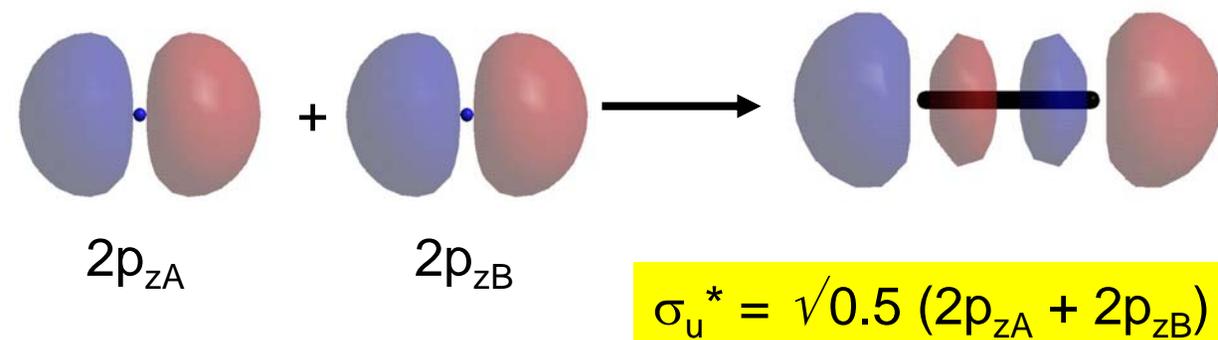
The shells below the valence shell will always contain an equal number of bonding and antibonding MO's so you only have to consider the MO's formed by the valence orbitals when you want to determine the bond order in a molecule!

Chem 59-250 Molecular Orbital Theory

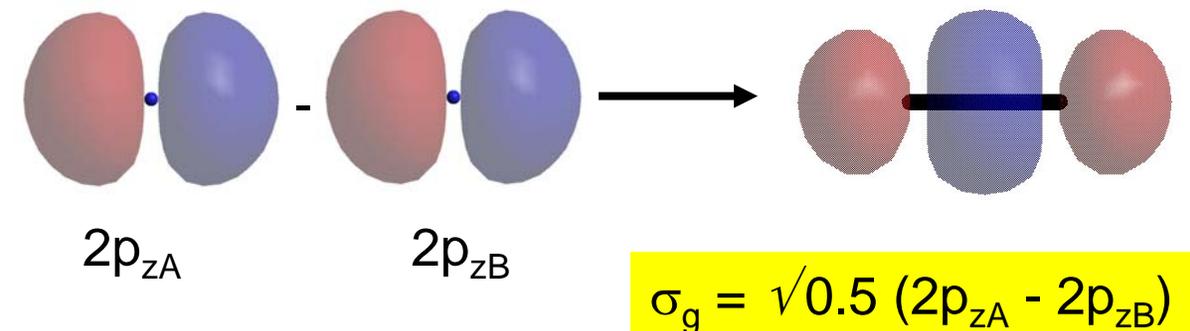
Diatomic molecules: The bonding in F_2

Each F atom has 2s and 2p valence orbitals, so to obtain MO's for the F_2 molecule, we must make linear combinations of each appropriate set of orbitals. In addition to the combinations of ns AO's that we've already seen, there are now combinations of np AO's that must be considered. The allowed combinations can result in the formation of either σ or π type bonds.

The combinations of σ symmetry:



This produces an MO over the molecule with a node between the F atoms. This is thus an antibonding MO of σ_u symmetry.

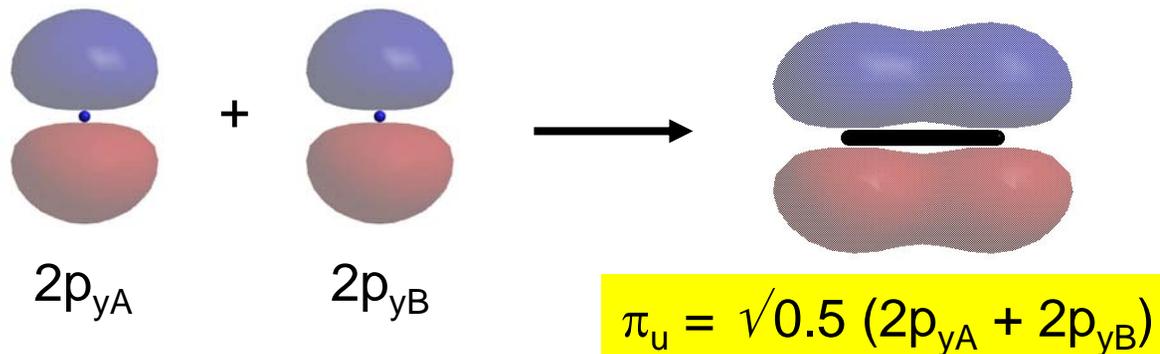


This produces an MO around both F atoms and has the same phase everywhere and is symmetrical about the F-F axis. This is thus a bonding MO of σ_g symmetry.

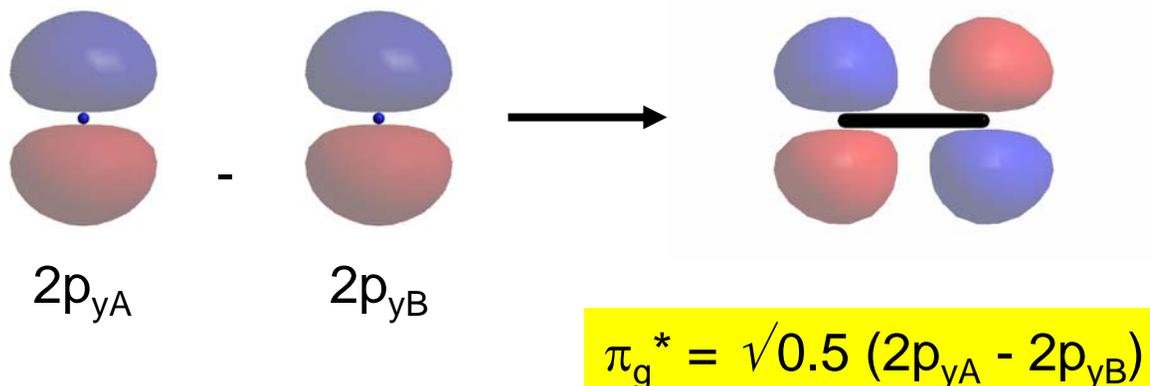
Chem 59-250 Molecular Orbital Theory

Diatomic molecules: The bonding in F_2

The first set of combinations of π symmetry:



This produces an MO over the molecule with a node on the bond between the F atoms. This is thus a bonding MO of π_u symmetry.

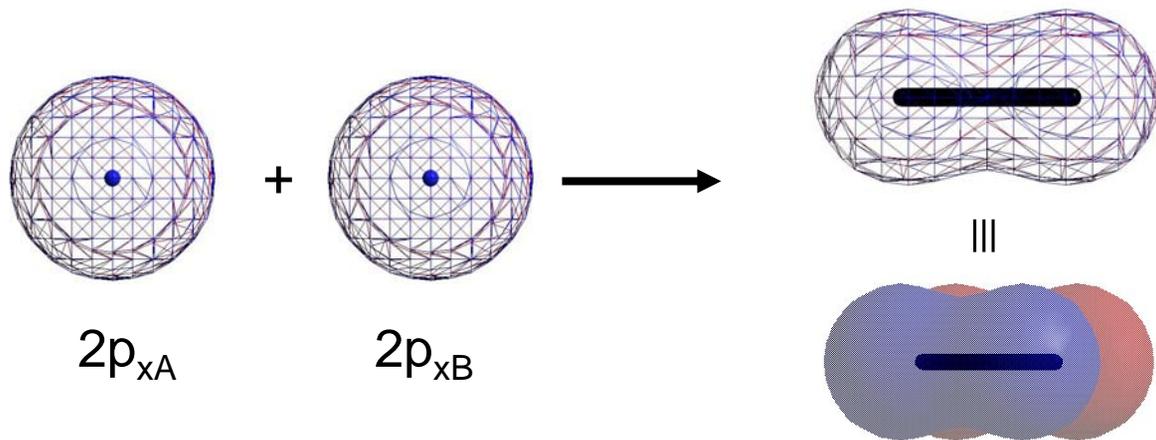


This produces an MO around both F atoms that has two nodes: one on the bond axis and one perpendicular to the bond. This is thus an antibonding MO of π_g symmetry.

Chem 59-250 Molecular Orbital Theory

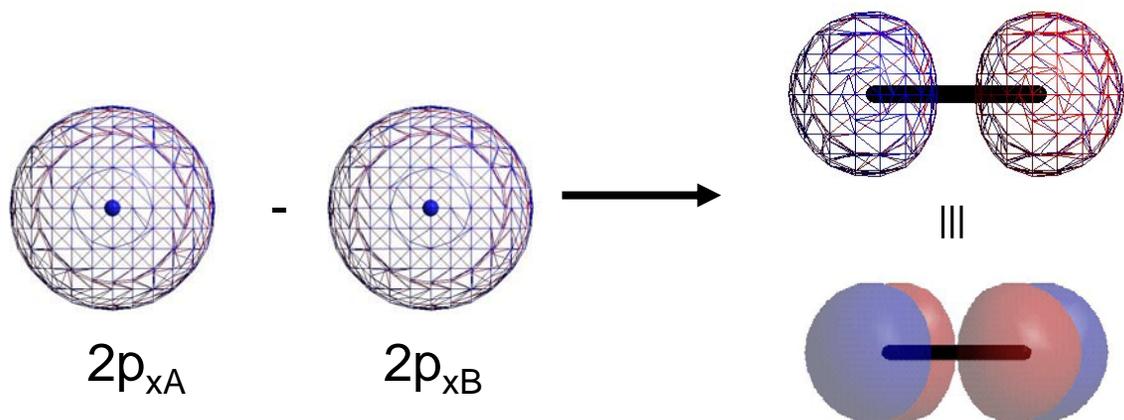
Diatomic molecules: The bonding in F_2

The second set of combinations with π symmetry (orthogonal to the first set):



This produces an MO over the molecule with a node on the bond between the F atoms. This is thus a bonding MO of π_u symmetry.

$$\pi_u = \sqrt{0.5} (2p_{xA} + 2p_{xB})$$

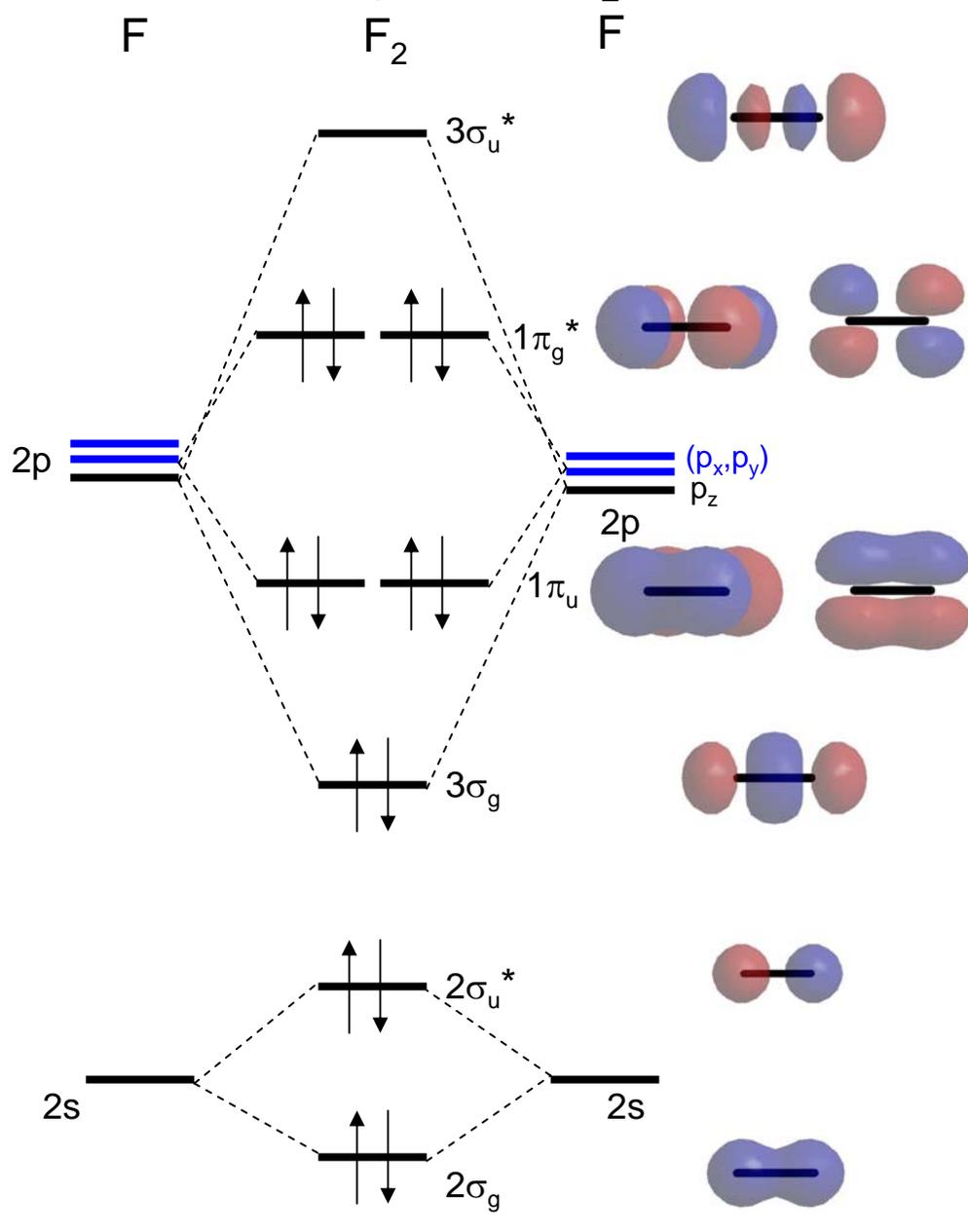


This produces an MO around both F atoms that has two nodes: one on the bond axis and one perpendicular to the bond. This is thus an antibonding MO of π_g symmetry.

$$\pi_g^* = \sqrt{0.5} (2p_{xA} - 2p_{xB})$$

Chem 59-250 Molecular Orbital Theory

MO diagram for F_2



You will typically see the diagrams drawn in this way. The diagram is only showing the MO's derived from the valence electrons because the pair of MO's from the 1s orbitals are much lower in energy and can be ignored.

Although the atomic 2p orbitals are drawn like this:  they are actually all the same energy and could be drawn like this: 

at least for two non-interacting F atoms.

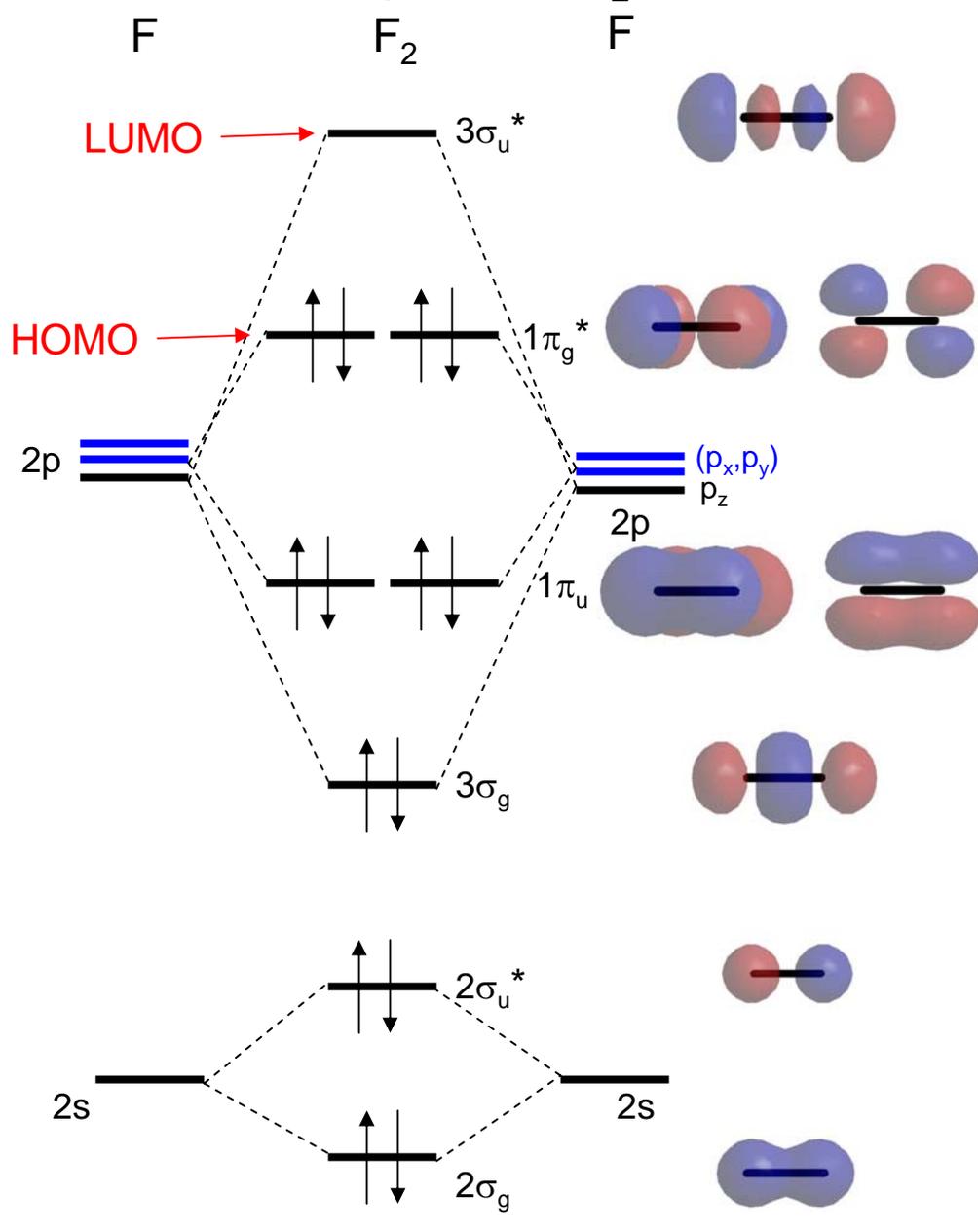
Notice that there is no mixing of AO's of the same symmetry from a single F atom because there is a sufficient difference in energy between the 2s and 2p orbitals in F.

Also notice that the more nodes an orbital of a given symmetry has, the higher the energy.

Note: The the sake of simplicity, electrons are not shown in the atomic orbitals.

Chem 59-250 Molecular Orbital Theory

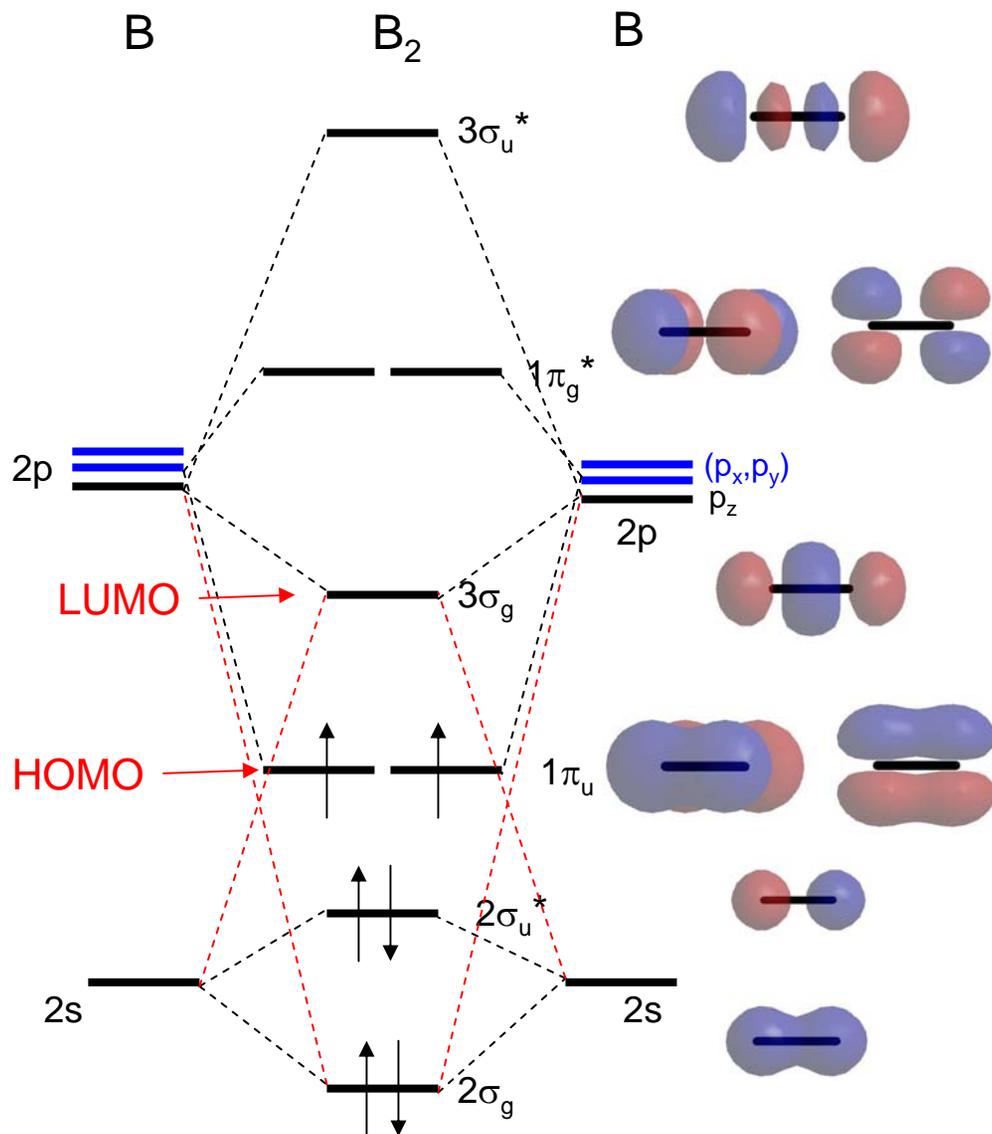
MO diagram for F₂



Another key feature of such diagrams is that the π -type MO's formed by the combinations of the p_x and p_y orbitals make degenerate sets (i.e. they are identical in energy).

The highest occupied molecular orbitals (HOMOs) are the $1\pi_g^*$ pair - these correspond to some of the "lone pair" orbitals in the molecule and this is where F₂ will react as an electron donor.

The lowest unoccupied molecular orbital (LUMO) is the $3\sigma_u^*$ orbital - this is where F₂ will react as an electron acceptor.

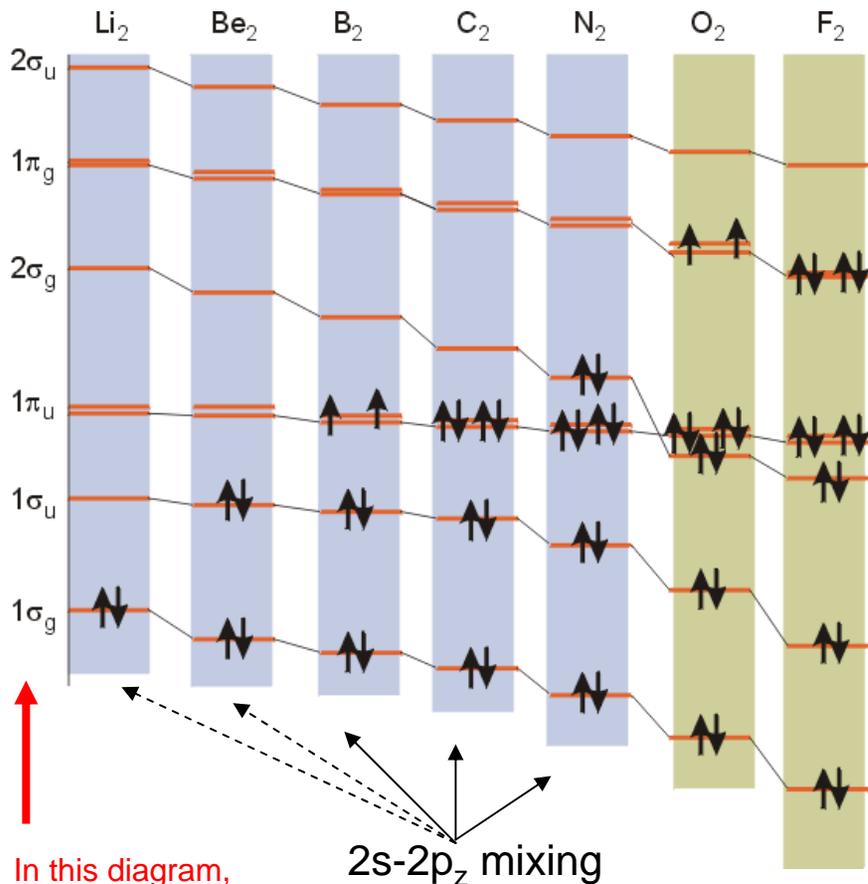
MO diagram for B_2 

In the MO diagram for B_2 , there are several differences from that of F_2 . Most importantly, the ordering of the orbitals is changed because of mixing between the $2s$ and $2p_z$ orbitals. From Quantum mechanics: the closer in energy a given set of orbitals of the same symmetry, the larger the amount of mixing that will happen between them. This mixing changes the energies of the MO's that are produced.

The highest occupied molecular orbitals (HOMOs) are the $1\pi_u$ pair. Because the pair of orbitals is degenerate and there are only two electrons to fill, them, each MO is filled by only one electron - remember Hund's rule. Sometimes orbitals that are only half-filled are called "singly-occupied molecular orbitals" (SOMOs). Since there are two unpaired electrons, B_2 is a **paramagnetic** (triplet) molecule.



Diatatomic molecules: MO diagrams for Li₂ to F₂



In this diagram, the labels are for the valence shell only - they ignore the 1s shell. They should really start at $2\sigma_g$ and $2\sigma_u^*$.

Remember that the separation between the ns and np orbitals increases with increasing atomic number. This means that as we go across the 2nd row of the periodic table, the amount of mixing decreases until there is no longer enough mixing to affect the ordering; this happens at O_2 . At O_2 the ordering of the $3\sigma_g$ and the $1\pi_u$ MO's changes.

As we go to increasing atomic number, the effective nuclear charge (and electronegativity) of the atoms increases. This is why the energies of the analogous orbitals **decrease** from Li_2 to F_2 .

The trends in bond lengths and energies can be understood from the size of each atom, the bond order and by examining the orbitals that are filled.

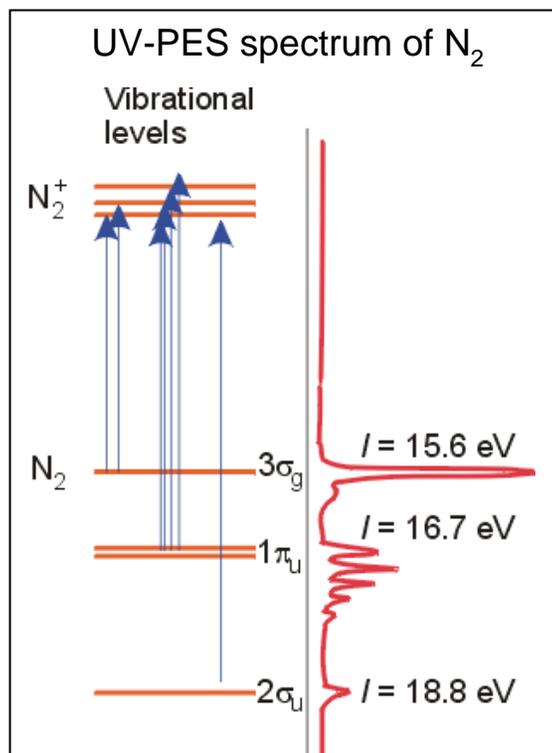
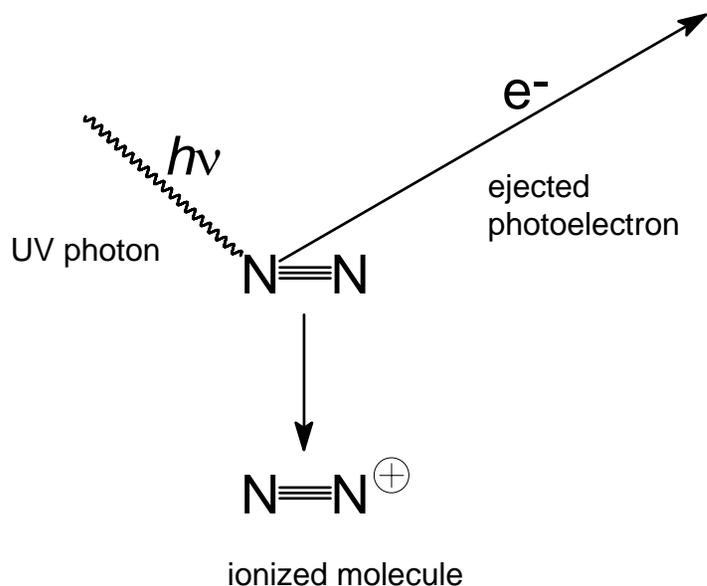
Molecule	Li ₂	Be ₂	B ₂	C ₂	N ₂	O ₂	F ₂	Ne ₂
Bond Order	1	0	1	2	3	2	1	0
Bond Length (Å)	2.67	n/a	1.59	1.24	1.01	1.21	1.42	n/a
Bond Energy (kJ/mol)	105	n/a	289	609	941	494	155	n/a
Diamagnetic (d)/ Paramagnetic (p)	d	n/a	p	d	d	p	d	n/a

Ultra-Violet Photoelectron Spectroscopy (UV-PES)

The actual energy levels of the MO's in molecules can be determined experimentally by a technique called photoelectron spectroscopy. Such experiments show that the MO approach to the bonding in molecules provides an excellent description of their electronic structure.

In the UV-PES experiment, a molecule is bombarded with high energy ultraviolet photons (usually $E_{\text{photon}} = h\nu = 21.1 \text{ eV}$). When the photon hits an electron in the molecule it transfers all the energy to the electron. Part of the energy (equal to the ionization potential, I , of the MO in which the electron was located) of the *photoelectron* is used to leave the molecule and the rest is left as kinetic energy (KE). The kinetic energy of the electrons are measured so I can be calculated from the equation:

$$I = h\nu - KE = 21.1 \text{ eV} - KE$$



The shape and number of the peaks provides other information about the type of orbital the photoelectron came from.

We will not worry about the details, but you can find out more about this in a course on spectroscopy.