

Assignment 2

Due: Tuesday, March 14

Question #1

1. A study of crystalline sample of molybdenum hexacarbonyl, $\text{Mo}(\text{CO})_6$, showed to be molecular and to crystallize in the space group $Pnma$ (No. 62). Discuss the possible locations and the symmetries of the molecules if there were: (i) 8 formula units per cell (ii) 4 formula units per cell (iii) 2 formula units per cell.

2. Me_3NHCl crystallizes in a monoclinic centrosymmetric space group, with $a = 6.09$, $b = 7.03$, $c = 7.03$ Å, $\beta = 95.73$ and $Z = 2$. The only limiting condition is $0k0$ $k = 2n$. What is the space group? Comment on the probable positions of (a) Cl (b) C (c) N (d) H atoms.

3. Calcium (Ca) crystallizes in a cubic space group with $a = 5.56$ Å and we observe a reflection corresponding to a d-spacing of 1.85 Å. What families of planes (hkl) could contribute to this reflection?

4. The default setting for the analysis software on the powder X-ray diffractometer lists peaks by their d-spacing instead of by their diffraction angle. Explain why d-spacing is a more useful default using a plane from Ca as an example.

5. For a primitive cubic lattice composed of only one type of atom:

- What are the positions of each of the atoms in the unit cell (using the standard setting with positions in fractional coordinates)?
- What fraction of each atom is contained within the unit cell?
- Using the information from (a) and (b), calculate the value of a general structure factor, $F(hkl)$, for this structure in terms of the atomic scattering factor f_{atom} . Remember that: $\exp(i\theta) = \cos(\theta) + i\sin(\theta)$.
- Comment on the importance/utility of your result in part (c).
- Calculate the general structure factor for a face-centered cubic lattice.

6. Tantalum (Ta) crystallizes in a cubic space group with $a = 3.3013$ Å. Reflections for the following families of planes are observed:

(110) , (200) , (211) , (220) , (310) , (222) , (321) , (400) , (411) , (420) , (332) , (431)

- What type of cubic lattice do these data imply?
- Which reflection (110) or (200) should be more intense? (note: just draw one representative plane for each (hkl) to help you make your decision)
- Determine the structure factors for the (110) and (200) planes. Note that the atomic scattering

factors in units of electrons are: $f_{Ta}(110) = 57$; $f_{Ta}(200) = 50$.

(d) Determine the structure factor for the (111) plane if $f_{Ta}(111) = 54$. Draw an Argand diagram to illustrate your result.

7. Determine the final magnitude $|F|$ and phase α obtained by the addition of the following atomic scattering factors (or waves) and draw an approximate Argand diagram to illustrate the process:

f_j	$\phi_j(^{\circ})$
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33	45
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9	120
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7	140
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7	-10
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7	180
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6	-90
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1	-110
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1	-100
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1	-105
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Comment briefly on the phase you have calculated.