

Assignment 1

Due: Feb. 16, 2017

Question #1

1. Consider an atom at fractional coordinates x, y, z . When operated on by the following symmetry elements, what are the fractional coordinates of the symmetry related atoms?

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|----------------------------|---------------------------------------|--------------------------------------|
| (a) 2 along b | (b) -4 along c | (c) m perpendicular to b |
| (d) -1 centered at (000) | (e) 4_3 along c | (f) b glide plane perpendicular to a |
| (g) 2_1 along a | (h) n glide plane perpendicular to b. | |

2. The compound $[\text{Cp}^*_3\text{Pb}_2][\text{B}(\text{C}_6\text{F}_5)_4]$ (MW = 1499.09) crystallizes in the space group $C2/c$ with $a = 22.545(5) \text{ \AA}$, $b = 14.773(5) \text{ \AA}$, $c = 17.087(5) \text{ \AA}$, $\beta = 114.911(5)$, $Z = 4$. Calculate the density of this salt and indicate if there are any other conclusions you can draw about the structure.

3. The ionic compound $[(\text{C}_{11}\text{H}_{20}\text{N}_2)_2\text{P}][\text{Cl}] \cdot n(\text{C}_7\text{H}_8)$ crystallizes in the space group $P-1$ with $a = 10.134(3)$, $b = 12.243(3)$, $c = 13.037(3) \text{ \AA}$, $\alpha = 103.358(4)$, $\beta = 99.906(5)$, $\gamma = 100.772(4)$. Given that the measured density is 1.145 g cm^{-3} what conclusions can you draw about the structure.

4. (a) Using diagrams explain why a B centered cell is not a distinct monoclinic cell.
(b) Using diagrams explain why an I centered monoclinic cell is equivalent to a C centered monoclinic cell.

5. Use diagrams to show and explain the relationship between $P2_1/n$ and $P2_1/c$.

6. For a primitive unit cell from each of the 7 crystal systems:

- (a) identify the point group of the unit cell (treat it as an isolated box)
(b) use drawing(s) to show the location of the symmetry elements of the cell (again for a box)

7. What systematic absences are expected if the following symmetry elements are present?

- (a) I centered lattice
(b) c glide perpendicular to a
(c) mirror perpendicular to b
(d) 2_1 along c

8. Explain in detail, the information implied by the space group symbol $Fd-3m$.

9. Identify the possible space groups implied by the following information. Also indicate if the space group is uniquely determined (see section 3.1 of the *International Tables for Crystallography Volume A*).

- (a) primitive monoclinic lattice, for $h0l$, $h00$, $00l$ present only for $l = 2n$.
- (b) primitive orthorhombic lattice, for $00l$, present only for $l = 2n$.
- (c) C centered orthorhombic lattice, no other absences observed.
- (d) F centered orthorhombic lattice, no other absences observed.
- (e) centrosymmetric C centered monoclinic lattice, no other absences observed.

10. At low temperatures, methane crystallizes in a cubic cell with $a = 5.89 \text{ \AA}$. Assuming that the density of the solid methane is similar to that of liquid methane ($d = 0.466 \text{ g cm}^{-3}$), determine whether methane adopts a primitive, body-centered or face-centered structure.

11. What are the Miller indices for planes with the following unit cell intercepts:

- (a) ∞a , $1/3 b$, c
- (b) a , b , c
- (c) $-1/4 a$, $1/2 b$, $3 c$
- (d) $1/6 a$, $1/3 b$, $3/4 c$
- (e) $2/3 a$, ∞b , $1/6 c$

12. Draw orthorhombic unit cells with dimensions of $a = 4 \text{ \AA}$, $b = 7 \text{ \AA}$ and $c = 9 \text{ \AA}$. Draw the following planes (make sure to label them): (100), (010), (001), (-210), (011), (111), (042), (222), (301), (024)

13. Determine the d-spacing for each family of planes in question 12.

14. Using $\text{MoK}\alpha$ X-rays, what would be diffraction angle for each family of planes in question 12.